There are many effective ways to represent a minimum free energy RNA secondary structure that make it easy to locate its helices and loops. It is a greater challenge to visualize the thermal average probabilities of all folds in a partition function sum; dot plot representations are often puzzling. Therefore, we introduce the RNAbows visualization tool for RNA base pair probabilities. RNAbows represent base pair probabilities with line thickness and shading, yielding intuitive diagrams. RNAbows aid in disentangling incompatible structures, allow comparisons between clusters of folds, highlight differences between wild type and mutant folds, and are also rather beautiful.

I. INTRODUCTION

Graphical representations can profoundly influence our conception of physical reality or interpretation of data. For example, in conventional representations of RNA secondary structure the stems (regions of stacked base pairs) and loops (gaps between) are easily identified; however, showing only one set of base pairs makes invisible the prevalence of thermal fluctuations. In fact, the likelihood of being in even the most probable structure is exceedingly small and thermal fluctuations allow the molecule to explore many states. To characterize RNA structures in thermal equilibrium, better visualization methods are needed.

Much work has gone into developing computational methods to predict the secondary structure from the sequence, including: minimizing free energy [1–3], computing the partition function [2–6], stochastically sampling the partition function [7], enumerating states [8], kinetic approaches [9, 10], maximum-expected accuracy approaches [11, 12], comparative analysis [13, 14], and statistical methods [15–17]. The accuracy of predictions has received scrutiny [18–21]. Our particular interest is to visualize ensembles of structural states in thermal equilibrium. To characterize RNA structures in thermal equilibrium, better visualization methods are needed.

A number of tools have also been developed to visualize RNA secondary structures. The minimum free energy (MFE) or other secondary structures can be depicted in two-dimensional “airport terminal” diagrams, in which the backbone defines the perimeter and lines or dots between bases denote the pairs, as in Figure 1(a). A classic “rainbow” diagram, see Figure 1(b), encodes the same information but instead of the backbone sequence forming the perimeter, it is stretched horizontally with the base pairs making long arcs. In circle diagrams [22], the backbone is arranged in a circle with arcs again marking the pairs. Most compact is bracket notation [6], see Figure 1(c), in which unpaired bases are periods and matching parentheses indicate paired bases. To represent non-nested pseudoknot structures, bracket notation requires additional delimiters, like [ ] or { }.

Partition-function based computational methods predict the thermal average probabilities \( P_{ij} \) of RNA base pairs rather than one single structure. The \( P_{ij} \) information is often represented in dot plots — a grid is made and the size or color of the dot at \( (i, j) \) indicates the probability of pairing base \( i \) with base \( j \), as in Figure 1(d,f). Dots along diagonals indicate stems.

Because the eye naturally groups similar objects together [23], the dot plot representation in Figure 1(d) subliminally suggests that each color represents a unique structure. But closer examination reveals, for example, that base 41 along the horizontal axis forms red pairs with bases 4, 9, 13, and 35 along the vertical axis. So if there is not a single red structure, can one figure out which dots are consistent?

The Figure 1(e) hybrid approach adds to the MFE structure a color coding of the bases according to their probability of pairing [24]. This approach may leave the impression of a single static structure in which the predictions vary in certainty, rather than of a fluctuating molecule exploring many states and many local minima.

II. RESULTS

We introduce RNAbows diagrams as a more intuitive way to visualize RNA structures in thermal equilibrium. RNAbows are the partition function analog of rainbow diagrams. In RNAbows diagrams, we use the line thickness and shade of the arcs to represent the probability of a base pair. The single AllPairs RNAbow displays the entire partition function. In Figure 1(g) it is simple to see the two local minima structures because the eye naturally groups parallel lines. With RNAbows our perceptual inclinations help us, rather than hinder us.

To facilitate comparisons at a glance we introduce the difference RNAbow diagram, such as Figures 1(h), 2, and 3. Two folds, top and bottom, are juxtaposed. Color highlights the differences between folds. When \( \top_{ij} > \bot_{ij} \) the top arc’s color is set proportional to the relative probability excess \( \delta_{ij} = (\top_{ij} - \bot_{ij}) \); otherwise \( \delta_{ij} = 0 \). We then either use the (hue, saturation,
FIG. 1: Depictions secondary structures for the *L. collosoma* Spliced Leader sequence: (a) two-dimensional “airport terminal” diagram of the Minimum Free Energy (MFE) state, (b) classic “rainbow” diagram (MFE), (c) bracket notation with periods representing unpaired bases and parentheses indicating paired bases (MFE). (d) A dot plot with partition function probabilities $P_{ij}$ with base $i$ vertical and base $j$ horizontal. Color is assigned on the basis of the logs of probabilities. [Graphics adapted from RNAstructure.] (e) ViennaRNA’s prediction (using slightly different free energy rules) with bases color coded according to their partition function probabilities. [Graphics adapted from ViennaRNA.] (f) A Dot Plot available from ViennaRNA uses box size proportional to probability (upper triangle), but the grid obscures low probability pairs. (g) An AllPairs RNAbow diagram with the line width and darkness proportional to the probability of the base pairs. (h) A Clusters RNAbow diagram after resolving into the two dominant clusters, with probability 0.57 (red) and 0.43 (blue); Note that the MFE state [Fig. 1(b)] belongs to the less probable blue cluster.

In Figure 1(g) we see two dominant structural classes in the total partition function. To visualize each local minima we first have to partition the partition function; we use our PF method, which is described fully in the Supplemental Information. The idea is to identify the base pair $(i,j)$ which is most incompatible with other base pairs. We then split the partition function into two, one with the $(i,j)$ pair *Prohibited* and one with the $(i,j)$ pair *Forced* to exist. The resulting $P$ and $F$ clusters

$$
(H, S, V) = (\text{red}, X_{ij}^{\text{top}}, X_{ij}^{\text{top}} - P_{ij}^{\text{top}} + 1),
$$
$$
(R, G, B) = (255 \cdot X_{ij}^{\text{top}} / P_{ij}^{\text{top}}, 0, 0),
$$
for pair $(i,j)$ on the top. Formulas for bottom arcs are analogous. Pairs with similar weight are colored black, extra weight drives top pairs toward red and bottom pairs toward blue.
FIG. 2: The partition functions of Wild Type (red) and the U22G mutant (blue) the 5′UTR of ferritin light chain mRNA are depicted. The colors are set proportional to the difference between the clusters such that common elements are black, while the distinct elements are either red or blue. The dramatic effect of this single nucleotide polymorphism on the secondary structure is evident. Other base changes within loop regions have less influence.

If desired, the $PF$ procedure could be repeated again on each cluster to further disentangle structures. Notice also in Figure 1(h) that the maximum probabilities $P_{ij}$ within each daughter cluster approach 1 while the most probable pair in the parent cluster was 0.57, roughly the weight $p_P$. It is easy to imagine applications to visualizing riboswitches which exhibit a conformational change between two folds.

In Figure 2, we present a Difference RNABow comparison of the 5′ UTR of Ferritin Light Chain wild type to the U22G mutant [25] associated with Hyperferritinemia cataract syndrome. This single nucleotide polymorphism dramatically changes the folding pattern. In particular, the loss of the Iron Response Element, the brightest red hairpin in Figure 2, disrupts binding by an iron-response
In Figure 3 we present a Difference RNABow which shows how information about which bases are unpaired obtained from chemical mapping experiments can be incorporated in partition function calculations.

![HIV 5' UTR](image)

FIG. 3: Chemical mapping experiments indicate which bases are unpaired, and this information can also be visualized with Difference RNABOWS. Here, for the 5'-UTR region of HIV-1, we compare the constrained [26] partition function where lower-case bases are forced to be unpaired (top, red) with the unconstrained partition function (bottom, blue).

III. ACCESS

From http://rna.williams.edu/ users can create their own RNABOWS with a choice of UNAFOLD, VIENNARNA, or RNASTRUCTURE [2, 3, 5] to compute the partition functions. Three RNABOWS tools are available:

**AllPairs** to visualize the entire partition function [Figure 1(g)] with base pairs denoted by arcs whose width and shading is proportional to the probability of the pair,

**Clusters** to split that partition function into two clusters [Figure 1(h)] using the PF method described in Supplemental Information, and

**Difference RNAbows** to highlight the differences between the partition functions of two sequences [Figures 1(h), 2, 3].

The RNABow graphics are rendered in EPS, PDF, or SVG formats for easy import into other applications. All graphics are vector based, so there is no image degradation at any scale.

Advanced users can also import $P_{ij}$ data they have pre-computed using other algorithms. Source code for RNAbows is also available by request for incorporation into other applications.

IV. CONCLUSION

Visualization tools can offer insights into problems beyond mere representation of data. With RNAbows, a partition function’s base pair probability information becomes easier to use and more powerful. Our instinctive pattern-matching ability allows us to quickly compare clusters of structures. Incompatible clusters can be disentangled by eye, or by the $PF$ procedure described.

The basic RNABowS tools are extensible to represent any data set with varying coupling strengths and then to highlight differences between conditions. The difference RNAbow juxtaposes arcs and highlights differences with color. The recent R-chie package [27] also uses double arcs to visualize helices predicted from multiple alignments with the Transat program [14]. Making side-by-side comparisons of multiple folds is less straightforward with dot plots.

Furthermore, the mental misconceptions that come from looking at a static MFE, PDB, or consensus structure — forgetting that thermal fluctuations open and close pairs, or forgetting that not all pairs are equally stable — are challenged subliminally by the gradations of the shadings in RNABow pairs.

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Supplemental Information

Here we will describe our approach to disentangle incompatible secondary structures, resulting in two clusters of compatible structures, as seen in Figure 1(h).

Most folding algorithms [1–6] use the set of nested structures to build their partition functions. In the partition function, it is possible to have two probable pairs $P_{ij}$ and $P_{kl}$ which are non-nested, see Figure 1(g), but non-nested pairs do not co-occur in any of the individual states in the partition function sum.

Non-nestedness of pairs is therefore a hallmark of the incompatibility of the structures.

In our simple and iterative $PF$ clustering method, we sum over non-nested ($k,l$) pairs to find the $(i,j)$ pair that produces the biggest non-nestedness score,

$$\psi_{ij} = P_{ij} \sum_{k<i<l<j} P_{kl} + P_{ij} \sum_{i<k<j<l} P_{kl}.$$  \hspace{1cm} (1)

Once the maximum $\psi_{ij}$ has been identified, we then perform a new partition function computation with bases $(i,j)$ forced to pair to create the Forced $F$ cluster.

The $F$ cluster is the portion of the original partition function that contains the $(i,j)$ pair. The $F$ cluster’s free energy

$$G_F = -RT \log \sum_{s \in F} e^{G_s},$$

and base pair probabilities $p_{ij}^F$ are output. The fraction of the original partition function is

$$p_F = \exp\{-(G_F - G_0)/kT\},$$

where $G_0$ is the original free energy. The original partition function minus the forced partition function leaves all states in which the $(i,j)$ pair is prohibited, the $P$ cluster. The values for the prohibited cluster $P$ can be obtained from the conservation of probability:

$$p_P = p_0 - p_F$$

and

$$p_F p_{ij}^P = p_0 p_{ij}^0 - p_F p_{ij}^F,$$

or by computing the partition function with a prohibit $(i,j)$ constraint.

It is clear from Figure 1(h) that the effect that forcing even one base pair can have in dividing the ensemble of structures is remarkable.

Our $PF$ procedure can also be repeated on any previously defined cluster as well at the root; each time separating further incompatibilities. The overall run time is $O(KN^3)$, where $K$ is the number of clusters. [The sums of Eq. (1) appear to require $O(N^4)$ operations if one sums over the indices; however, by iterating over a list of the $O(N)$ base pairs which exceed a probability threshold, $P_{ij} > \theta \sim 10^{-6}$, Eq. (1) requires only $O(N^2)$ operations.] A detailed description of our related Nestor algorithm, which instead creates clusters from stochastically sampled states, is also forthcoming.